

- a. Taking logarithms of both sides of the Cobb-Douglas production function, we get

$$\ln Q_t = \alpha + \beta \ln K_t + \gamma \ln L_t + u_t$$

- b. Let  $\alpha = \alpha_1 + \alpha_2 t$ ,  $\beta = \beta_1 + \beta_2 t$ , and  $\gamma = \gamma_1 + \gamma_2 t$ . Substituting these in the basic model, we obtain the unrestricted model.

$$\ln Q_t = \alpha_1 + \alpha_2 t + \beta_1 \ln K_t + \beta_2 (t \ln K_t) + \gamma_1 \ln L_t + \gamma_2 \ln (t L_t) + v_t$$

- c. The variables to be generated are:  $\ln Q_t$ ,  $\ln K_t$ ,  $\ln L_t$ ,  $t \ln K_t$ , and  $t \ln L_t$ .
- d. The null hypothesis is  $\alpha_2 = \beta_2 = \gamma_2 = 0$ . The alternative is that at least one of these coefficients is not zero.
- e. The test statistic is  $F_c = \frac{(ESSR - ESSU)/3}{ESSU/(46-6)}$ , where ESSR and ESSU are the error sums of squares for the restricted and unrestricted models, respectively.
- f. Under the null  $F_c$  has the  $F$ -distribution with 3 d.f. for the numerator and 40 d.f. for the denominator.
- g. The critical value is  $F_{3,40}^*(0.05) = 2.84$ .
- h. Reject the null hypothesis if  $F_c > 2.84$ .